# **EXPERIMENT P8: SINGLE-PHASE TRANSFORMER**

Related course: KIE3009 (Energy Conversion and High Voltage Transmission)

# **OBJECTIVES:**

- 1. To determine the turns ratio and the equivalent circuit parameters of a transformer from the open and short-circuit tests
- 2. To perform a load test with a resistive and a capacitive load and predict the results from the equivalent circuit

# **EQUIPMENT:**

Transformer, voltmeter, ammeter, resistive load, capacitive load

# **INSTRUCTIONS:**

- 1. Record all your results and observations in a log book / paper
- 2. Follow the experiment procedure properly

# **REFERENCE(S):**

Refer to the main references of KIE3009

# **TEST:**

TEST 1: Open-Circuit Test (no load test) TEST 2: Short-Circuit Test (full load test) TEST 3: Load Test

# **INTRODUCTION**

A transformer is an electrical device designed on the concept of magnetic coupling. It uses magnetically coupled coils to transfer energy from one circuit to another. In power systems, it is used for stepping up or down the AC voltage or current. In electronic circuits (e.g. radio, TV), it is used for impedance matching, isolating one part of a circuit from another and stepping up or down AC voltage and current.

For transformers operating at 50 or 60 Hz in power systems, they can handle several hundred megawatts of power and weigh a hundred tons. In communication system, microwatts of power are involved and the frequency is hundreds of megacycles but the physical dimensions of the transformers are only fractions of an inch. Although the principles of operation are the same, the constructions vary widely.

### **Transformer equivalent circuit**

An ideal transformer has no resistance and the magnetic material of the core has infinite permeability, no saturation, no hysteresis, no eddy currents under alternating magnetisation, no internal power dissipation, the voltage level is changed by the turns ratio and the instantaneous input and output power is always equal (efficiency  $= 100\%$ ).

In real transformers, the resistance of the windings and the losses in the core absorb some of the input power. Hence, the efficiency of a real transformer is not 100%. Since air is not a magnetic insulator, some of the flux leaks out of the iron and therefore, the two windings are not linked by exactly the same amount of flux. To indicate that the characteristics of a real transformer are related to an ideal transformer, a real transformer can be represented by an equivalent circuit as shown in Fig. 1.

 $(N_1/N_2)^2R_2$ 

 $V_2' = (N_1/N_2)V_2$  $I_2 = (N_2/N_1)I_2$ 

 $(N_1/N_2)^2 X_2$ 

2

2



Fig.1: Equivalent circuit of a real transformer

where

 $X_1$ ,  $X_2$  = leakage reactance (represents voltage drop due to flux leakage)  $R_1$ ,  $R_2$  = winding resistance  $X_m$  = magnetising reactance *R<sup>c</sup>* = resistance representing core losses  $I_0$  = no-load current  $I_m$  = magnetising current  $I_c$  = eddy current and hysteresis loss in the core  $I_2$ <sup> $I_2$ </sup> = current to neutralize secondary Magnetomotive force (mmf)  $V_1$  = primary voltage  $k =$  turns ratio of the ideal transformer  $= N_1/N_2 = V_1/V_2 = I_2/I_1$  $R_{e1}$  = equivalent primary resistance referred to primary side  $X_{e1}$  = equivalent primary reactance referred to primary side  $Z_{e1} = R_{e1} + jX_{e1}$  $X_{e1} = X_1 + (N_1 / N_2)^2 X$  $R_{e1} = R_1 + (N_1 / N_2)^2 R$  $V_1 = V_2 + (R_{e1} + jX_{e1})I_2$ 

When the real transformer is supplying a load,  $I_2$ ' and  $I_2$  in the equivalent circuit are no longer zero and the series resistance  $R_{e1}$  and  $X_{e1}$  represent the loss produced by the current in the transformer. As the transformer is loaded, the secondary voltage does not remain constant. Due to the power loss in *R<sup>e</sup>*1, the output power is less than the input power.

### **Transformer Regulation**

The equivalent circuit parameters can be used to deduce the voltage regulation of the transformer (i.e. variation of the secondary voltage with secondary current for constant primary voltage). This deduction can be easily made by referring to the vector diagram shown in Fig. 2 (developed from Fig. 1). Since the voltage drops in  $R_{e1}$  and  $X_{e1}$  are very small compared to  $V_1$  and  $V_2$ , the angle  $\theta$  is very small. Therefore,

$$
V_1 = V_2' + R_{e1} l_2' \cos \phi + X_{e1} l_2' \sin \phi = V_2 / k + k l_2 (R_{e1} \cos \phi + X_{e1} \sin \phi)
$$
 (1)



Fig 2: Transformer vector diagram

### **TEST 1: Open-Circuit Test (no load test)**

The open-circuit test is performed to find the ideal turns ratio  $k = V_1/V_2$  and to study the magnetising current *Im*. The secondary side of the transformer is left open. Connecting a voltmeter across the secondary side does not complete the current path. If the wattmeter reading (iron core loss) is taken with  $V_1$  at its rated value,  $R_c$  and  $X_m$  of the equivalent circuit could be obtained.

#### **PROCEDURES:**

- 1. For open-circuit test, connect the circuit as shown in Fig. 3. The metal frame of the transformer should be connected to the variac earth. The variable voltage AC supply is taken from a variable autotransformer, referred to as a "Variac."
- 2. Set the primary voltage *V*<sup>1</sup> (using variac) to 0, 40, 80, 120, 160, 200 and 240V. For each  $V_1$ , record the primary current  $I_1$  using ammeter and secondary voltage  $V_2$  using voltmeter. Record the results in a table with columns of  $V_1$ ,  $I_1$  and  $V_2$ .
- 3. Then, for each pair of  $V_1$  and  $V_2$ , calculate the turns ratio  $k = V_1 / V_2$ .

**Notes:** When using the variac, it is important that the variac is set to 0V before the main supply switch is turned on and it is returned to 0V before the supply switch is turned OFF. The voltage scale and pointer on the variac gives only an approximate indication of voltage and should not be used as a substitute for voltmeter readings.



Fig. 3: Open-Circuit Test

### **TEST 2: Short-Circuit Test (full load test)**

The short circuit test is performed to calculate the ideal turns ratio  $k = I_2 / I_1$  and to find the value of *R<sup>e</sup>*<sup>1</sup> and *X<sup>e</sup>*<sup>1</sup> (the series impedance referred to the primary side). The secondary side of the transformer is short-circuited using an ammeter. If the wattmeter reading (copper loss) is taken with  $I_2$  at its rated value,  $R_{e1}$  and  $X_{e1}$  could be calculated.

### **PROCEDURES:**

- 1. Calculate the rated current *I*<sup>2</sup> from the information given in the transformer nameplate data. The nameplate data can be seen on top of the transformer. Hint:  $S = V_2 l_2$ , where *S* is the transformer power in VA and  $V_2$  is the secondary voltage in Volt.
- 2. For short-circuit test, connect the circuit as shown in Fig. 4.
- 3. When the secondary side is short-circuited, the voltage  $V_1$  required to produce the rated current is much lower than the normal operating voltages. It is therefore very
- 4. Set the primary voltage  $V_1$  (using variac) to 0, 1, 2, 3, 4 and 5V. For each  $V_1$ , record the primary current  $I_1$  and secondary current  $I_2$  using ammeter. Record the results in a table with columns of  $V_1$ ,  $I_1$  and  $I_2$ .
- 5. Then, for each pair of  $I_1$  and  $I_2$ , calculate the turns ratio  $k = I_2 / I_1$ .



Fig. 4: Short-Circuit Test

#### **TEST 3: Load Test**

#### **PROCEDURES:**

- 1. Connect the circuit as shown in Fig. 5. For the load, use a purely resistive load.
- 2. Set the primary voltage  $V_1$  to 240V by using the variac. Adjust the load so that the secondary current  $I_2$  is as minimum as possible. Record  $I_2$ ,  $I_1$  and  $V_2$  in a table.
- 3. Keeping *V*<sup>1</sup> constant at 240V, adjust the resistive load so that *I*<sup>2</sup> increases by 0.1 A. Record  $I_2$ ,  $I_1$  and  $V_2$ .
- 4. Repeat step 3 until the resistive load reaches the minimum point.
- 5. Switch OFF the power supply. Change the load to a purely capacitive load.
- 6. Keeping *V*<sup>1</sup> constant at 240V, turn ON one switch of the capacitive load and record *I*2,  $I_1$  and  $V_2$ . Turn ON another switch of the capacitive load and record  $I_2$ ,  $I_1$  and  $V_2$ . Repeat this step until all switches are turned ON.



Fig. 5: Load Test

### **QUESTIONS:**

# **A. Open Circuit Test (TEST 1)**

- 1. Sketch a simplified equivalent circuit of the transformer at open-circuit test.
- 2. From your table, plot  $V_1$  (on y-axis) against the current  $I_1$  and calculate turns ratio  $k =$ *V*1/*V*<sup>2</sup> for each *I*1. Analyse and discuss your results.
- 3. From no. 2, notice that the current  $I_1$  is not a linear function of  $V_1$ . Explain why.
- 4. What value is the transformer turns ratio *k*? (take the average value)
- 5. If  $P_{\text{oc}} = 8.5$  Watt, which represents the iron core loss and  $V_1 = 240V$ , using  $I_1$  value from your results, show that the magnetising current *I<sup>m</sup>* is approximately equal to *I*1. Hint: Use  $P_{oc} = V_1 I_1 \cos \phi$  to find  $\phi$ , then use it in  $I_m = I_1 \sin \phi$

# **B. Short-circuit Test (TEST 2)**

- 1. Sketch a simplified equivalent circuit of the transformer at short-circuit test.
- 2. Plot *V*<sup>1</sup> against *I*1. Analyse and discuss your results.
- 3. What value is the turns ratio *k* (take the average value)? Compare this *k* from the open-circuit test.
- 4. From your  $V_1$  vs.  $I_1$  graph, determine the value of  $Z_{e1} = V_1 / I_1$ . Then, given that the primary and secondary winding resistance  $R_1$  and  $R_2$  as 1.9 and 0.05 Ω respectively, calculate  $R_{e1}$ . After that, calculate  $X_{e1}$  using  $X_{e1}$  = sqrt( $Z_{e1}^2 - R_{e1}^2$ ).

# **C. Load Test (TEST 3)**

- 1. Plot the secondary voltage *V*<sup>2</sup> against secondary current *I*<sup>2</sup> for each resistive load and capacitive load on separate graphs. Analyse and discuss your results.
- 2. Using  $V_1$ =240V, the calculated values of  $R_{e1}$  and  $X_{e1}$  from TEST 2, the average value of *k* from TEST 1 or 2 and using equation (1), determine the regulation characteristic equation  $V_2$  for the purely resistive load ( $\phi = 0^\circ$ ) and purely capacitive load ( $\phi = -90^\circ$ ). Hint: Find equation of  $V_2$  in term of  $I_2$  from equation (1).
- 3. Plot  $V_2$  vs.  $I_2$  from question C2 on the same graph plotted in question C1. If there is a difference between the predicted value (from question C2) and the actual value (from question C1), explain why.
- 4. Is the flux in the transformer core change considerably from no-load to full-load? Why?

### **END OF EXPERIMENT**